



Roll No. _____ to be filled in by the candidate.

(For all sessions)

Paper Code

6

1

9

3

Mathematics (Objective Type)

Time: 30 Minutes

Marks: 20

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A, B, C & D to each question are given. Which answer you consider correct, fill the corresponding circle A, B, C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. The fraction $\frac{2x^2 + 5}{x - 3}$ is:

- (A) proper (B) rational (C) polynomial (D) improper

2. $(n+1)^{\text{th}}$ term of an A-P is:

- (A) $a_1 + (n-1)d$ (B) $a_1 - (n-1)d$ (C) $a_1 + nd$ (D) $a_1 - nd$

3. Multiplicative inverse of $(1, 0)$ is:

- (A) $(-1, 0)$ (B) $(0, 1)$ (C) $(0, -1)$ (D) $(1, 0)$

4. If $a, b \in G$ and G is a group, then $(ab)^{-1}$ is equal to:

- (A) $a^{-1}b^{-1}$ (B) $b^{-1}a^{-1}$ (C) $\frac{-1}{ab}$ (D) $\frac{1}{(ab)^{-1}}$

5. If A is a subset of B and $A=B$ then A is:

- (A) proper subset of B (B) super set of B (C) improper subset of A (D) proper subset of A

6. Rank of $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ is:

- (A) 1 (B) 2 (C) 3 (D) 4

7. If A and B are any two non singular matrices then $(AB)^{-1}$ is equal to:

- (A) $A^{-1}B^{-1}$ (B) $B^{-1}A^{-1}$ (C) BA (D) AB

8. An equation of the form $ax^2 + bx + c = 0$ is called quadratic if:

- (A) $a = 0$ (B) $b = 0$ (C) $c = 0$ (D) $a \neq 0$

9. The roots of $x^2 + 2x + 3 = 0$ are:

- (A) imaginary (B) real, equal (C) real, unequal (D) rational

10. $\cos^{-1}(-x)$ is equal to:
- (A) $\cos^{-1} x$ (B) $\pi + \cos^{-1} x$ (C) $\pi - \cos^{-1} x$ (D) $\sin^{-1} x$
11. Number of solutions of trigonometric equation is:
- (A) finite (B) infinite (C) only one (D) all of these
12. The 5th term of sequence 3, 6, 12,..... is:
- (A) $\frac{1}{48}$ (B) -48 (C) $-\frac{1}{48}$ (D) 48
13. For two events A and B if $P(A) = P(B) = \frac{1}{2}$, then $P(A \cap B)$ is:
- (A) $\frac{1}{4}$ (B) $\frac{1}{2}$ (C) 1 (D) Zero
14. $\frac{3}{0}$ equals.
- (A) 3 (B) 6 (C) ∞ (D) 12
15. Middle term of $(a+b)^n$, when n is even is:
- (A) $\left(\frac{n}{2}+1\right)^{\text{th}}$ term (B) $\left(\frac{n}{2}-1\right)^{\text{th}}$ term (C) $\frac{n}{2}$ th term (D) $\left(\frac{n}{2}-2\right)^{\text{th}}$ term
16. The sum of binomial co-efficients in the expansion of $(1+x)^4$ is:
- (A) 8 (B) 10 (C) 16 (D) 32
17. $1 + \tan^2 \theta$ is equal to:
- (A) $\cot \theta$ (B) $\operatorname{cosec} \theta$ (C) $\sec^2 \theta$ (D) $-\sec \theta$
18. $\tan\left(\frac{3\pi}{2} - \theta\right)$ is equal to:
- (A) $\tan \theta$ (B) $-\cot \theta$ (C) $\cot \theta$ (D) $-\tan \theta$
19. Period of $\tan \frac{x}{2}$ is:
- (A) π (B) 2π (C) $\frac{\pi}{2}$ (D) $\frac{3\pi}{2}$
20. In any triangle ABC, with usual notations r_3 is:
- (A) $\frac{\Delta}{S-a}$ (B) $\frac{S-b}{\Delta}$ (C) $\frac{S-c}{\Delta}$ (D) $\frac{\Delta}{S-c}$

Roll No. _____ to be filled in by the candidate.

(For all sessions)

Paper Code 6 0 1 9

Mathematics (Essay Type)

Time: 2:30 Hours

Marks: 80

Section -I

2. Write short answers of any eight parts from the following.

2x8=16

i. Prove the rule of addition $\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$.

ii. Simplify i^9 .

iii. Write any two proper subsets of a set $\{a, b, c\}$.

iv. Define a semi group.

v. Without expansion show that:
$$\begin{vmatrix} 6 & 7 & 8 \\ 3 & 4 & 5 \\ 2 & 3 & 4 \end{vmatrix} = 0$$

vi. Evaluate $(1+w-w^2)^8$

vii. Write the converse and the inverse of the conditional $\sim p \rightarrow q$ viii. For $A = \{1, 2, 3, 4\}$, find a relation $R = \{(x, y) / y = x\}$.ix. By remainder theorem find remainder when $x^2 + 3x + 7$ is divided by $x + 1$.x. If A is symmetric or Skew symmetric. Show that A^2 is symmetric.

xi. Find x and y if
$$\begin{bmatrix} x+3 & 1 \\ -3 & 3y-4 \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ -3 & 2 \end{bmatrix}$$
.

xii. If α, β be the roots of $x^2 - px - p - c = 0$, prove that $(1+\alpha)(1+\beta) = 1-c$.

3. Write short answers of any eight parts from the following.

2x8=16

i. Resolve $\frac{1}{x^2-1}$ into partial fractions.

ii. Insert two G.Ms between 2 and 16.

iii. Find the value of n , when ${}_{12}C_n = {}_6C_n$.iv. Evaluate 9P_8 .v. Expand upto 4 terms $(1-x)^{1/2}$.vi. Calculate by means of binomial theorem, $(0.97)^3$.vii. Write the first four terms of the sequence if $a_n = na_{n-1}, a_1 = 1$.viii. If 5, 8 are two A.Ms between a and b find a and b .ix. If $\frac{1}{k}, \frac{1}{2k+1}$ and $\frac{1}{4k-1}$ are in H.P, find k .

x. Define probability and sample space.

xi. Determine the probability of getting 2 heads in two successive tosses of a balanced coin.

xii. Prove that $1+5+9+\dots+(4n-3) = n(2n-1)$ for $n=1, 2$.

4. Write short answers of any nine parts from the following.

2x9=18

i. Find r , when $l = 56cm$ $\theta = 45^\circ$.ii. Prove that: $\frac{1+\cos\theta}{1-\cos\theta} = (\operatorname{cosec}\theta + \cot\theta)^2$.iii. Prove that: $\tan(45^\circ + A)\tan(45^\circ - A) = 1$.iv. Prove that: $\frac{\cos 3\theta}{\cos\theta} + \frac{\sin 3\theta}{\sin\theta} = 4\cos 2\theta$.

- v. Find period of $\operatorname{cosec} \frac{x}{4}$.
- vi. Prove that: $\frac{\sin \alpha - \sin \beta}{\sin \alpha + \sin \beta} = \tan \frac{\alpha - \beta}{2} \cot \frac{\alpha + \beta}{2}$.
- vii. If α, β, γ are the angles of a triangle ABC, then prove that $\cos(\alpha + \beta) = -\cos \gamma$.
- viii. When the angle between the ground and the sun is 30° , flag pole casts a shadow of 40m long.
Find the height of the top of the flag.
- ix. Find the measure of greatest angle if the sides of triangle are 16, 20, 33.
- x. Find the area of the triangle ABC, if $a = 18, b = 24, c = 30$.
- xi. Show that: $\tan^{-1}(-x) = -\tan^{-1} x$.
- xii. Find the solution of the equation $\sin x = -\frac{\sqrt{3}}{2}$ lie in $[0, 2\pi]$.
- xiii. Find solution of $\sec x = -2$ in $[0, 2\pi]$.

Section -II

Note: Attempt any three questions from the following.

10x3=30

5. (a) Solve the system of linear equation by Cramer's rule $2x + 2y + z = 3$; $3x - 2y - 2z = 1$; $5x + y - 3z = 2$.

(b) Solve the equation: $x^{\frac{2}{5}} + 8 = 6x^{\frac{1}{5}}$.

6. (a) Resolve $\frac{4x}{(x+1)^2(x-1)}$ into partial fractions.

(b) If a, b, c, d , are in G.P prove that $a^2 - b^2, b^2 - c^2, c^2 - d^2$ are also in G.P.

7. (a) Two dice are thrown. What is the probability that the sum of the number of dots appearing on them is 4 or 6.

(b) Find the general term in the expansion of $(1+x)^{-3}$, when $|x| < 1$.

8. (a) Find the values of trigonometric functions, when $\theta = \frac{13\pi}{3}$. (b) Prove that: $\frac{\cos 8^\circ - \sin 8^\circ}{\cos 8^\circ + \sin 8^\circ} = \tan 37^\circ$.

9. (a) Show that: $\gamma = \alpha \sin \frac{\beta}{2} \sin \frac{\gamma}{2} \sec \frac{\alpha}{2}$. (b) Prove that: $2 \tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{7} = \frac{\pi}{4}$.



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(For all sessions)

Paper Code 6 1 9 1

Mathematics (Objective Type)

Time: 30 Minutes

Marks: 20

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A, B, C & D to each question are given. Which answer you consider correct, fill the corresponding circle A, B, C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. If Z is a complex number, then $|Z|^2$ is:

(A) Z^2

(B) $(\bar{Z})^2$

(C) $Z\bar{Z}$

(D) $\frac{Z}{\bar{Z}}$

2. For any two sets A and B , $(A \cap B)'$ is equal to:

(A) A'

(B) B'

(C) $A' \cup B'$

(D) $A \cap B$

3. The multiplicative identity in the set of real numbers is:

(A) Zero

(B) 1

(C) 3

(D) 2

4. A square matrix $A = [a_{ij}]$ with complex entries is called skew Hermitian if $(\bar{A})^t$ is equal to:

(A) A

(B) $-A$

(C) $|A|$

(D) $-|A|$

5. If A and B are any two non singular matrices such that $(AB)^{-1}$ is equal to:

(A) $A^{-1}B^{-1}$

(B) $B^{-1}A^{-1}$

(C) BA

(D) AB

6. A reciprocal equation remains unchanged when variable x is replaced by:

(A) $\frac{1}{x}$

(B) $\frac{-1}{x}$

(C) $\frac{1}{x^2}$

(D) $-x$

7. The roots of equation $x^2 - 5x + 6 = 0$ are:

(A) 2, -3

(B) -2, -3

(C) 2, 3

(D) -2, 3

8. $(x-1)^2 = x^2 - 2x + 1$ is called:

(A) equation

(B) conditional

(C) identity

(D) fraction

9. A.M between $3\sqrt{5}$ and $5\sqrt{5}$ is:

(A) $4\sqrt{5}$

(B) $5\sqrt{5}$

(C) 10

(D) $2\sqrt{5}$

10. n^{th} term of G.P is:

- (A) $a_1 r^n$ (B) $a_1 r^{n-1}$ (C) $\frac{a}{r^n}$ (D) $\frac{r^n}{a}$

11. If $n = 1$, then value of $n \binom{n-1}{r}$ is:

- (A) Zero (B) 1 (C) 2 (D) -1

12. $\sum_{r=0}^n \binom{n}{r}$ equals.

- (A) 1 (B) n (C) zero (D) 2

13. General term of expansion $(a+x)^n$ is:

- (A) $\binom{n+1}{r} a^{n-r} x^r$ (B) $\binom{n}{r-1} a^{n-r} x^r$ (C) $\binom{n}{r+1} a^r x^{n-r}$ (D) $\binom{n}{r} a^{n-r} x^r$

14. The sum of binomial co-efficients in the expansion of $(1+x)^4$ is:

- (A) 8 (B) 10 (C) 16 (D) 32

15. $\cos^2 2\theta + \sin^2 2\theta$ is equal to:

- (A) 1 (B) zero (C) $\sec^2 \theta$ (D) 2

16. $\cos\left(\frac{\pi}{2} - \beta\right)$ is equal to:

- (A) $\sin \beta$ (B) $-\sin \beta$ (C) $\cos \beta$ (D) $-\cos \beta$

17. Period of $\operatorname{cosec} 10x$ is:

- (A) $\frac{\pi}{10}$ (B) $\frac{2\pi}{5}$ (C) $\frac{\pi}{5}$ (D) $\frac{4\pi}{5}$

18. For any triangle ABC, with usual notations r_2 is equal to:

- (A) $\frac{\Delta}{S-a}$ (B) $\frac{\Delta}{S-c}$ (C) $\frac{\Delta}{S-b}$ (D) $\frac{\Delta}{S}$

19. $\tan(\sin^{-1} x)$ is equal to:

- (A) $1+2x^2$ (B) $1-x^2$ (C) $\frac{x}{\sqrt{1-x^2}}$ (D) $\frac{2x}{\sqrt{1+x^2}}$

20. The solutions of equation $\frac{1}{2} + \sin \theta = 0$ are in quadrant.

- (A) I & IV (B) I & III (C) III & IV (D) II & IV

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Paper Code 6 0 1 9

Mathematics (Essay Type)

Time: 2:30 Hours

Marks: 80

Section -I

2. Write short answers of any eight parts from the following.

2x8=16

- i. Find the multiplicative inverse of $(-4, 7)$.
- ii. Find real and imaginary parts of $(\sqrt{3} + i)^3$.
- iii. Define equivalent sets.
- iv. Define monoid.
- v. Find the inverse of the matrix $A = \begin{bmatrix} 3 & -1 \\ 2 & 1 \end{bmatrix}$.
- vi. Show that $\begin{vmatrix} 1 & 2 & 3x \\ 2 & 3 & 6x \\ 3 & 5 & 9x \end{vmatrix} = 0$, without expansion.
- vii. Find the value of λ if $A = \begin{bmatrix} 4 & \lambda & 3 \\ 7 & 3 & 6 \\ 2 & 3 & 1 \end{bmatrix}$ is singular.
- viii. Define exponential equation.
- ix. If $U = \{1, 2, 3, \dots, 10\}$, $A = \{2, 4, 6, \dots, 20\}$ and $B = \{1, 3, 5, \dots, 19\}$, prove that $(A \cup B)' = A' \cap B'$.
- x. Write converse and contrapositive of the conditional $Nq \rightarrow Np$.
- xi. Find three cube-cube roots of unity.

xii. If α, β are the roots of $3x^2 - 2x + 4 = 0$, find the values of $\frac{1}{\alpha^2} + \frac{1}{\beta^2}$.

3. Write short answers of any eight parts from the following.

2x8=16

- i. Resolve $\frac{1}{(x-1)(2x-1)}$ into partial fractions.
- ii. Which term of the A.P 5, 2, -1, ... is -85.
- iii. Find the value of n if ${}^n P_4 : {}^{n-1} P_3 = 9 : 1$.
- iv. Find the number of diagonals of 12 sided figure.
- v. Find the first four terms of $(1+2x)^{-1}$.
- vi. Find the 6th term in the expansion of $\left(x^2 - \frac{3}{2x}\right)^{10}$.
- vii. Find the next two terms of the sequence 1, -3, 5, -7, 9, -11,
- viii. If 5, 8 are two A.Ms between a and b find a and b .
- ix. Convert the recurring decimal $2.\dot{2}\dot{3}$ into the equivalent common fraction.
- x. Convert $n(n-1)(n-2)\dots(n-r+1)$ in the factorial form.
- xi. How many numbers greater than 1000,000 can be formed from digits 0, 2, 2, 2, 3, 4, 4.
- xii. Show that inequality $4^n > 3^n + 4$ is true for $n = 2, 3$.

4. Write short answers of any nine parts from the following.

2x9=18

- i. Verify $2 \sin 45^\circ + \frac{1}{2} \operatorname{cosec} 45^\circ = \frac{3}{\sqrt{2}}$.
- ii. Prove that: $\cot^2 \theta - \cos^2 \theta = \cot^2 \theta \cos^2 \theta$.
- iii. Find the value of $\tan 75^\circ$ (without calculator).
- iv. Prove that: $\cos 306^\circ + \cos 234^\circ + \cos 162^\circ + \cos 18^\circ = 0$.

- v. Prove that $\sqrt{\frac{1+\sin\alpha}{1-\sin\alpha}} = \frac{\sin\frac{\alpha}{2} + \cos\frac{\alpha}{2}}{\sin\frac{\alpha}{2} - \cos\frac{\alpha}{2}}$.
- vi. Prove that: $\sin\left(\frac{\pi}{4} - \theta\right)\sin\left(\frac{\pi}{4} + \theta\right) = \frac{1}{2}\cos 2\theta$.
- vii. Find the period of $\operatorname{cosec}\frac{x}{4}$.
- viii. Show that: $\tan(\sin^{-1}x) = \frac{x}{\sqrt{1-x^2}}$.
- ix. Prove that $abc(\sin\alpha + \sin\beta + \sin\gamma) = 4\Delta S$.
- x. Define trigonometric equation.
- xi. Find the area of triangle ABC, if $a = 524$, $b = 276$, $c = 315$.
- xii. Find the smallest angle of the triangle ABC, when $a = 37.34$, $b = 3.24$, $c = 35.06$.
- xiii. Find the solution of $\sec x = -2$ which lies in $[0, 2\pi]$.

Section -II

Note: Attempt any three questions from the following.

10x3=30

5. (a) Use Cramer's rule to solve the system $2x + 2y + z = 3$; $3x - 2y - 2z = 1$; $5x + y - 3z = 2$.

- (b) If α and β are the roots of $x^2 - 3x + 5 = 0$ form the equation whose roots are $\frac{1-\alpha}{1+\alpha}$ and $\frac{1-\beta}{1+\beta}$.

6. (a) Resolve into partial fractions. $\frac{x^2}{(x-1)^2(x+1)}$.

- (b) For what value of n $\frac{a^n + b^n}{a^{n-1} + b^{n-1}}$ is G.M between a and b .

7. (a) How many arrangements of the letters of the word ATTACKED can be made if each arrangement begins with C and ends with K.

- (b) Find the co-efficient of x^5 in the expansion of $\left(x^2 - \frac{3}{2x}\right)^{10}$.

8. (a) Prove the identity $\sin^6\theta - \cos^6\theta = (\sin^2\theta - \cos^2\theta)(1 - \sin^2\theta\cos^2\theta)$.

- (b) If $\sin\alpha = \frac{4}{5}$ and $\cos\beta = \frac{40}{41}$ where $0 < \alpha < \frac{\pi}{2}$ and $0 < \beta < \frac{\pi}{2}$ show that $\sin(\alpha - \beta) = \frac{133}{205}$.

9. (a) The sides of a triangle are $x^2 + x + 1$, $2x + 1$ and $x^2 - 1$ prove that the greater angle of the triangle is 120° .

- (b) Prove that $\tan^{-1}\frac{1}{11} + \tan^{-1}\frac{5}{6} = \tan^{-1}\frac{1}{3} + \tan^{-1}\frac{1}{2}$.



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Paper Code	6	1	9	1
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Mathematics (Objective Type)**Group-I**

Time: 30 Minutes

Marks: 20

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given. Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. $\overline{-a-ib}$ equals:

- (A) $a+ib$ (B) $-a+ib$ (C) $a-ib$ (D) $-a-ib$

2. w^3 equals:

- (A) 0 (B) -1 (C) i (D) 1

3. Sum of complex roots of unity equals:

- (A) 0 (B) -1 (C) 1 (D) w

4. $(z, +)$ has no identity other than:

- (A) 1 (B) -1 (C) i (D) 0

5. $(AB)^{-1}$ equals:

- (A) $A^{-1}B^{-1}$ (B) $A^{-1}B$ (C) B^{-1} (D) $B^{-1}A^{-1}$

6. $[8]$ is a:

- (A) square matrix (B) unit matrix (C) scalar matrix (D) rectangular matrix

7. Partial fractions of $\frac{x^2+1}{(x+1)(x-1)}$ will be of the form:

- (A) $\frac{A}{x+1} + \frac{B}{x-1}$ (B) $\frac{Ax+B}{x+1} + \frac{C}{x-1}$ (C) $1 + \frac{A}{x+1} + \frac{B}{x-1}$ (D) $\frac{Ax+B}{x^2-1}$

8. G.M between $2i$ and $8i$ equals:

- (A) ± 4 (B) 4 (C) -4 (D) $\pm 4i$

9. No term in G.P is:

- (A) 3 (B) 2 (C) 1 (D) 0

10. A die is rolled then $n(s)$ equals:

- (A) 36 (B) 6 (C) 1 (D) 9

11. The factorial form of 6.5.4 is:

- (A) $\frac{6!}{3!}$ (B) $6!$ (C) $3!$ (D) $\frac{6!}{2!}$

12. In the expansion of $(3+x)^4$ middle term will be:

- (A) 81 (B) $54x^2$ (C) $26x^2$ (D) x^4

13. The sum of odd coefficients in the expansion of $(1+x)^5$ is:

- (A) 16 (B) 32 (C) 25 (D) 5

14. One radian equals:

- (A) 45° (B) 50° (C) 60° (D) 57.296°

15. $\sin \theta$ equals:

- (A) $2\sin^2 \frac{\theta}{2}$ (B) $2\sin \frac{\theta}{2} \cos \frac{\theta}{2}$ (C) $2\cos^2 \frac{\theta}{2}$ (D) $2\tan \frac{\theta}{2}$

16. Period of $\tan \frac{x}{3}$ is:

- (A) π (B) 2π (C) 3π (D) $\frac{\pi}{2}$

17. Number of elements of a triangle are:

- (A) 3 (B) 4 (C) 6 (D) 8

18. Radius of inscribed circle is:

- (A) $\frac{\Delta}{S}$ (B) $\frac{S}{\Delta}$ (C) $\frac{\Delta}{S-c}$ (D) $\frac{4\Delta}{abc}$

19. $2 \tan^{-1} A$ equals:

- (A) $\tan^{-1} \left(\frac{A}{1-A^2} \right)$ (B) $\tan^{-1} \left(\frac{2A}{1+A^2} \right)$ (C) $\tan^{-1} \left(\frac{-2A}{1+A^2} \right)$ (D) $\tan^{-1} \left(\frac{2A}{1-A^2} \right)$

20. If $\cos x = \frac{\sqrt{3}}{2}$, $x \in [0, \pi]$, then x equals:

- (A) $\frac{-\pi}{6}$ (B) $\frac{5\pi}{6}$ (C) $\frac{\pi}{6}$ (D) $\frac{7\pi}{6}$

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Mathematics (Essay Type)**Group-I**

Time: 2:30 Hours

Marks: 80

Section -I

2. Write short answers of any eight parts from the following.

2x8=16

i. Show that $\forall z \in \mathbb{C} \quad z^2 + z^{-2}$ is a real number.ii. Simplify by justifying each step $\frac{\frac{1}{a} - \frac{1}{b}}{1 - \frac{1}{a} \cdot \frac{1}{b}}$.iii. Write down the power set of $\{9, 11\}$.iv. Solve by using quadratic formula $15x^2 + 2ax - a^2 = 0$ v. Convert $(A \cap B)' = A' \cup B'$ into logic form.vi. If a, b are elements of a group G, solve $ax = b$.vii. Show that $\begin{vmatrix} 2 & 3 & 0 \\ 3 & 9 & 6 \\ 2 & 15 & 1 \end{vmatrix} = 9 \begin{vmatrix} 2 & 1 & 0 \\ 1 & 1 & 2 \\ 2 & 5 & 1 \end{vmatrix}$ viii. Prove that $\left(\frac{1+\sqrt{-3}}{2}\right)^9 + \left(\frac{1-\sqrt{-3}}{2}\right)^9 = -2$.ix. Simplify $(5, -4) \div (-3, -8)$ x. If $A = \begin{bmatrix} 1 & 2 \\ a & b \end{bmatrix}$ and $A^2 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$, find the values of a and b.xi. If the matrices A and B are symmetric and $AB=BA$. Show that AB is symmetric.xii. Show that roots of $(p+q)x^2 - px - q = 0$ are rational.

3. Write short answers of any eight parts from the following.

2x8=16

i. Resolve $\frac{1}{x^2-1}$ into partial fractions.

ii. Find next two terms of sequence -1, 2, 12, 40,

iii. Find A.M between $x-3$ and $x+5$.

iv. Write 8.7.6.5 in the factorial form.

v. Evaluate 12P_5 .vi. If ${}^nC_8 = {}^nC_{12}$ find n.vii. Find vulgar fraction equivalent to 0.7^0 recurring decimal.viii. If the numbers $\frac{1}{k}, \frac{1}{2k+1}$ and $\frac{1}{4k-1}$ are in Harmonic sequence, find k.

ix. Determine the probability of getting 2 heads in two successive tosses of a balanced coin.

x. Show that ${}^nC_4 > {}^nC_{3+4}$ is not true for $n=1$.xi. Calculate $(2.02)^4$ by means of binomial theorem.xii. Expand $(1+2x)^{-1}$ upto four terms.

4. Write short answers of any nine parts from the following.

2x9=18

i. Convert $18^0 6' 21''$ to decimal form.ii. Prove that: $\cos^2 \theta - \sin^2 \theta = \cos^4 \theta - \sin^4 \theta$.iii. Find the value of $\tan 105^0$ (without calculator).iv. Prove that: $\frac{\sin 3x - \sin x}{\cos x - \cos 3x} = \cot 2x$.

- v. Find the value of $\sec(-300^\circ)$ (without table).
- vi. Find the domain and range of $\sec x$.
- vii. Define angle of elevation.
- viii. The area of triangle is 2437 and $a = 79, c = 97$, find β .
- ix. Show that $\tan(\sin^{-1} x) = \frac{x}{\sqrt{1-x^2}}$.
- x. Define trigonometric equation.
- xi. Verify $\sin^2 \frac{\pi}{6} : \sin^2 \frac{\pi}{4} : \sin^2 \frac{\pi}{3} : \sin^2 \frac{\pi}{2} = 1 : 2 : 3 : 4$.
- xii. A kite is flying at a height of 67.2m is attached to a fully stretched string inclined at an angle of 55° to the horizontal. Find the length of the string.
- xiii. Solve $\sin x + \cos x = 0$, where x lies in $[0, 2\pi]$.

Section -II

Note: Attempt any three questions from the following.

10x3=30

5. (a) If $A = \begin{bmatrix} i & 1+i \\ 1 & -i \end{bmatrix}$, show that $A + (\overline{A})^t$ is Hermitian.
- (b) If the roots of $px^2 + qx + q = 0$, are α and β , then prove that $\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} + \sqrt{\frac{q}{p}} = 0$.
6. (a) Resolve $\frac{x^2}{(x-2)(x-1)^2}$ into partial fractions. (b) Insert five Harmonic means between $\frac{1}{4}$ and $\frac{1}{24}$.
7. (a) Find the value of n and r , when ${}^nC_r = 35$ and ${}^nP_r = 210$.
- (b) Identify the series $1 + \frac{1}{3} + \frac{1}{3.6} + \frac{1}{3.6.9} + \dots$ as a Binomial expansion and find its sum.
8. (a) If $\operatorname{cosec} \theta = \frac{m^2 + 1}{2m}$ and $m > 0, \left(0 < \theta < \frac{\pi}{2}\right)$ find the values of the remaining trigonometric ratios.
- (b) Reduce $\sin^4 \theta$ to an expression involving only function of multiples of θ , raised to the first power.
9. (a) Solve the triangle using first law of tangent and then law of sines $a = 319, b = 168, r = 110^\circ 22'$.
- (b) Prove that $\sin^{-1} \frac{77}{85} - \sin^{-1} \frac{3}{5} = \cos^{-1} \frac{15}{17}$.

10. If A and B are disjoint events, then $P(A \cup B)$ equals:

- (A) $P(A) + P(B)$ (B) $P(A) + P(B) - P(A \cap B)$ (C) $P(A) + P(B) + P(A \cap B)$ (D) $P(A) - P(B)$

11. If two dice are thrown simultaneously, then the number of elements in the sample space are:

- (A) 6 (B) 12 (C) 24 (D) 36

12. The number of terms in the expansion of $(1+x)^{1/2}$, $|x| < 1$ are:

- (A) 2 (B) n (C) $\frac{n}{2}$ (D) infinite

13. If n is positive integer, then $n^2 > n+3$ is true when:

- (A) $n \geq 3$ (B) $n \geq 2$ (C) $n \geq 1$ (D) $n \leq 3$

14. $\cot^2 \theta - \operatorname{cosec}^2 \theta$ equals:

- (A) 1 (B) -1 (C) $\cot \theta$ (D) $\operatorname{cosec} \theta$

15. $\frac{3\pi}{2} + \theta$ lies in:

- (A) 1st quadrant (B) 2nd quadrant (C) 3rd quadrant (D) 4th quadrant

16. Period of $\cos \frac{x}{2}$ is:

- (A) π (B) 2π (C) 4π (D) $\frac{\pi}{2}$

17. With usual notations, in any triangle ABC, if $\Delta = 20$, $a=4$, $b=6$, $c=10$, then r equals:

- (A) 2 (B) 5 (C) 10 (D) 15

18. $\sin \left(\sin^{-1} \left(\frac{1}{2} \right) \right)$ equals:

- (A) $\frac{\pi}{3}$ (B) $\frac{\pi}{6}$ (C) $\frac{1}{2}$ (D) $\frac{\sqrt{3}}{2}$

19. With usual notations, r_1 equals:

- (A) $\frac{\Delta}{s}$ (B) $\frac{\Delta}{s-a}$ (C) $\frac{\Delta}{s-b}$ (D) $\frac{\Delta}{s-c}$

20. If $\sin x = -\frac{\sqrt{3}}{2}$, then reference angle is:

- (A) $\frac{\pi}{6}$ (B) $-\frac{\pi}{6}$ (C) $\frac{\pi}{3}$ (D) $-\frac{\pi}{3}$

Roll No. _____ to be filled in by the candidate.

(For all sessions)

Mathematics (Essay Type)**Group-II**

Time: 2:30 Hours

Marks: 80

Section -I

2. Write short answers of any eight parts from the following.

2x8=16

- i. Simplify $(a+ib)^3$.
- ii. If $B=\{1,2,3\}$, find the power set of B.
- iii. Define the conjunction.
- iv. Define the identity matrix.
- v. If $z = a+ib$ show that $(z - \bar{z})^2$ is real number.
- vi. Show that $x^3 + y^3 = (x+y)(x+wy)(x+w^2y)$.
- vii. Evaluate the determinant of $A = \begin{bmatrix} 1 & -2 & 3 \\ 2 & 3 & 1 \\ 4 & -3 & 2 \end{bmatrix}$.
- viii. If $A = \begin{bmatrix} 1 & -1 \\ a & b \end{bmatrix}$ and $A^2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ find the values of a and b.
- ix. Does the set $\{0, -1\}$ have closure property w.r.t addition and multiplication?
- x. Solve the equation by completing square $x^2 - 3x - 648 = 0$.
- xi. If a, b are elements of a group G, then show that $(ab)^{-1} = b^{-1}a^{-1}$.
- xii. If α, β are the roots of the equation $3x^2 - 2x + 4 = 0$, find the values of $\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$.

3. Write short answers of any eight parts from the following.

2x8=16

- i. Define proper rational fraction.
- ii. Write next two terms of -1, 2, 12, 40,
- iii. If $s_n = n(2n-1)$, then find the series.
- iv. Insert two G.Ms between 1 and 8.
- v. Expand $(1-x)^{1/2}$ upto 4 terms.
- vi. Prove that ${}^n C_r = {}^n C_{n-r}$.
- vii. How many 5-digit multiples of 5 can be formed from the digits 2, 3, 5, 7, 9 (no digit repeated).
- viii. Determine the probability of getting 2 heads in two successive tosses of a balanced coin.
- ix. A die is rolled. Find the probability that the dots on top are prime numbers or odd numbers.
- x. Show that $1 + 5 + 9 + \dots + (4n-3) = n(2n-1)$ is true for $n=1$ and $n=2$.
- xi. Using binomial theorem find the value of $\sqrt{99}$.
- xii. Find the General term of $\left(\frac{a}{2} - \frac{2}{a}\right)^6$.

4. Write short answers of any nine parts from the following.

2x9=18

- i. Convert $54^\circ 45'$ into radians.
- ii. Find x , if $\tan^2 45^\circ - \cos^2 60^\circ = x \sin 45^\circ \cos 45^\circ \tan 60^\circ$.
- iii. Prove that: $\frac{1}{1+\sin\theta} + \frac{1}{1-\sin\theta} = 2\sec^2\theta$.
- iv. Prove that: $\cot(\alpha + \beta) = \frac{\cot\alpha \cot\beta - 1}{\cot\alpha + \cot\beta}$.

- v. Find the value of $\sin 105^\circ$.
- vi. Express $\cos(x+y)\sin(x-y)$ as sum or difference.
- vii. Find the period of $\sin \frac{x}{5}$.
- viii. State the law of cosine.
- ix. Show that: $\frac{1}{r} = \frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3}$.
- x. Find domain and range of $y = \cos^{-1} x$.
- xi. Solve the equation $1 + \cos x = 0$.
- xii. Find the solution of $\sec x = -2$, $x \in [0, 2\pi]$.
- xiii. Find the area of the triangle ABC in which $a=18$, $b=24$, $c=30$.

Section -II

Note: Attempt any three questions from the following.

10x3=30

5. (a) Show that
$$\begin{vmatrix} a+\lambda & b & c \\ a & b+\lambda & c \\ a & b & c+\lambda \end{vmatrix} = \lambda^2(a+b+c+\lambda)$$

(b) If α and β are the roots of $5x^2 - x - 2 = 0$ form the equation roots are $\frac{3}{\alpha}$ and $\frac{3}{\beta}$.

6. (a) Resolve $\frac{1}{(x-3)^2(x+1)}$ into partial fractions.

(b) If the (Positive) G.M and H.M between two numbers are 4 and $\frac{16}{5}$, find the numbers.

7. (a) How many numbers greater than one million can be formed from the digits 0,2,2,2,3,4,4?

(b) Find the co-efficient of the term involving x^{-1} in the expansion of $\left(\frac{3x}{2} - \frac{1}{3x}\right)^{11}$.

8. (a) Prove that: $\frac{\tan \theta + \sec \theta - 1}{\tan \theta - \sec \theta + 1} = \tan \theta + \sec \theta$.

(b) Prove that: $\frac{\sin \alpha - \sin \beta}{\sin \alpha + \sin \beta} = \tan \frac{\alpha - \beta}{2} \cot \frac{\alpha + \beta}{2}$.

9. (a) Prove that in an equilateral triangle $r : R : r_1 = 1 : 2 : 3$.

(b) Prove that $\sin^{-1} \frac{5}{13} + \sin^{-1} \frac{7}{25} = \cos^{-1} \frac{253}{325}$.



Roll No. _____ to be filled in by the candidate.

(For all sessions)

Paper Code 6 1 9 5

Mathematics (Objective Type)

Time: 30 Minutes

Marks: 20

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A, B, C & D to each question are given. Which answer you consider correct, fill the corresponding circle A, B, C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. If n is a positive even integer, then $\binom{n}{1} + \binom{n}{3} + \binom{n}{5} + \dots + \binom{n}{n-1}$ is equal to:

- (A) 2^n (B) 2^{n+1} (C) 2^{n-1} (D) 3^n

2. An angle in the standard position whose terminal side falls on x -axis or y -axis is:

- (A) General angle (B) coterminal angle (C) Quadrantal angle (D) acute angle

3. $\cos(\pi + \theta)$ is equal to:

- (A) $\sec \theta$ (B) $-\cos \theta$ (C) $\cos \theta$ (D) $-\sec \theta$

4. Range of Cosine function is:

- (A) $(-1, 1)$ (B) $[-1, 1]$ (C) $[-1, 1)$ (D) $(-1, 1]$

5. In any ΔABC $r_1 r_2 r_3 =$ _____

- (A) Δ^4 (B) Δ^3 (C) Δ^2 (D) Δ

6. With usual notation $\sqrt{\frac{(s-b)(s-c)}{bc}}$ is equal to:

- (A) $\cos \frac{\alpha}{2}$ (B) $\sin \frac{\alpha}{2}$ (C) $\sin \frac{\beta}{2}$ (D) $\sin \frac{\gamma}{2}$

7. $\cos^{-1}(-x)$ is equal to:

- (A) $\frac{\pi}{2} - \sin^{-1} x$ (B) $\frac{\pi}{2} + \sin^{-1} x$ (C) $\pi + \cos^{-1} x$ (D) $\pi - \cos^{-1} x$

8. Solution of the equation $\tan x + 1 = 0$ is:

- (A) $\left\{ \frac{3\pi}{4} + n\pi \right\}$ (B) $\left\{ \frac{\pi}{4} + n\pi \right\}$ (C) $\{ \pi + n\pi \}$ (D) $\{ 2\pi + n\pi \}$, when $n \in \mathbb{Z}$

9. If $z = a + ib$, what is the value of $\cos \theta$?

- (A) $\frac{a}{|z|}$ (B) $\frac{b}{|z|}$ (C) $\frac{a}{b}$ (D) $\frac{b}{a}$

10. A function $f: A \rightarrow B$ is surjective if:
- (A) Range $f = A$ (B) Range $f = B$ (C) Range $f \neq B$ (D) Range $f \neq A$
11. Determinant of any unit matrix has value:
- (A) Greater than 1 (B) less than 1 (C) 1 (D) zero
12. A square matrix A is skew-symmetric if A' is equal to:
- (A) A (B) -A (C) A' (D) A^2
13. The discriminant of $ax^2 + bx + c = 0$, $a \neq 0$ is:
- (A) $b^2 + 4ac$ (B) $4ac - b^2$ (C) $b^2 - 4ac$ (D) $a^2 - 4ac$
14. The degree of the equation $x^3 + 3x^2 + 4x + 5 = 0$ is
- (A) 4 (B) 3 (C) 2 (D) 1
15. $\frac{x^2 + 1}{Q(x)}$ will be improper fraction if
- (A) Degree of $Q(x) = 2$ (B) Degree of $Q(x) = 3$
(C) Degree of $Q(x) = 4$ (D) Degree of $Q(x) = 5$
16. $\sum_{k=1}^n K$ is equal to:
- (A) $\frac{n+1}{2}$ (B) $\frac{n}{2}$ (C) $\frac{n(n+1)}{2}$ (D) $\frac{n(n-1)}{2}$
17. The geometric mean between -2^i and 8^i is:
- (A) ± 1 (B) ± 2 (C) ± 3 (D) ± 4
18. If A and B are mutually exclusive events, then $P(A \cup B)$ is equal to:
- (A) $P(A) + P(B)$ (B) $P(A) - P(B)$ (C) $P(AB)$ (D) $P(A) \cap P(B)$
19. If ${}^n C_8 = {}^n C_{12}$, then n is equal to:
- (A) 8 (B) 12 (C) 20 (D) 0
20. In the expansion of $(x + y)^8$, middle term is:
- (A) T_4 (B) T_6 (C) T_3 (D) T_5



Roll No. _____ to be filled in by the candidate.

(For all sessions)

Paper Code

6

1

9

7

Mathematics (Objective Type)

Time: 30 Minutes

Marks: 20

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A, B, C & D to each question are given. Which answer you consider correct, fill the corresponding circle A, B, C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. The geometric mean between $-2i$ and $8i$ is:

- (A) ± 1 (B) ± 2 (C) ± 3 (D) ± 4

2. If A and B are mutually exclusive events, then $P(A \cup B)$ is equal to:

- (A) $P(A) + P(B)$ (B) $P(A) - P(B)$ (C) $P(AB)$ (D) $P(A) \cap P(B)$

3. If ${}^n C_8 = {}^n C_{12}$, then n is equal to:

- (A) 8 (B) 12 (C) 20 (D) 0

4. In the expansion of $(x + y)^8$, middle term is:

- (A) T_4 (B) T_6 (C) T_3 (D) T_5

5. If n is a positive even integer, then $\binom{n}{1} + \binom{n}{3} + \binom{n}{5} + \dots + \binom{n}{n-1}$ is equal to:

- (A) 2^n (B) 2^{n+1} (C) 2^{n-1} (D) 3^n

6. An angle in the standard position whose terminal side falls on x -axis or y -axis is:

- (A) General angle (B) coterminal angle (C) Quadrantal angle (D) acute angle

7. $\cos(\pi + \theta)$ is equal to:

- (A) $\sec \theta$ (B) $-\cos \theta$ (C) $\cos \theta$ (D) $-\sec \theta$

8. Range of Cosine function is:

- (A) $(-1, 1)$ (B) $[-1, 1]$ (C) $|-1, 1)$ (D) $(-1, 1]$

9. In any ΔABC $r_1 r_2 r_3 =$ _____

- (A) Δ^4 (B) Δ^3 (C) Δ^2 (D) Δ

10. With usual notation $\sqrt{\frac{(s-b)(s-c)}{bc}}$ is equal to:

(A) $\cos \frac{\alpha}{2}$

(B) $\sin \frac{\alpha}{2}$

(C) $\sin \frac{\beta}{2}$

(D) $\sin \frac{\gamma}{2}$

11. $\cos^{-1}(-x)$ is equal to:

(A) $\frac{\pi}{2} - \sin^{-1} x$

(B) $\frac{\pi}{2} + \sin^{-1} x$

(C) $\pi + \cos^{-1} x$

(D) $\pi - \cos^{-1} x$

12. Solution of the equation $\tan x + 1 = 0$ is:

(A) $\left\{ \frac{3\pi}{4} + n\pi \right\}$

(B) $\left\{ \frac{\pi}{4} + n\pi \right\}$

(C) $\{ \pi + n\pi \}$

(D) $\{ 2\pi + n\pi \}$, when $n \in \mathbb{Z}$

13. If $z = a + ib$, what is the value of $\cos \theta$?

(A) $\frac{a}{|z|}$

(B) $\frac{b}{|z|}$

(C) $\frac{a}{b}$

(D) $\frac{b}{a}$

14. A function $f: A \rightarrow B$ is surjective if:

(A) Range $f = A$

(B) Range $f = B$

(C) Range $f \neq B$

(D) Range $f \neq A$

15. Determinant of any unit matrix has value:

(A) Greater than 1

(B) less than 1

(C) 1

(D) zero

16. A square matrix A is skew-symmetric if A' is equal to:

(A) A

(B) -A

(C) A'

(D) A^2

17. The discriminant of $ax^2 + bx + c = 0$, $a \neq 0$ is:

(A) $b^2 + 4ac$

(B) $4ac - b^2$

(C) $b^2 - 4ac$

(D) $a^2 - 4ac$

18. The degree of the equation $x^3 + 3x^2 + 4x + 5 = 0$ is

(A) 4

(B) 3

(C) 2

(D) 1

19. $\frac{x^2 + 1}{Q(x)}$ will be improper fraction if

(A) Degree of $Q(x) = 2$

(B) Degree of $Q(x) = 3$

(C) Degree of $Q(x) = 4$

(D) Degree of $Q(x) = 5$

20. $\sum_{k=1}^n K$ is equal to:

(A) $\frac{n+1}{2}$

(B) $\frac{n}{2}$

(C) $\frac{n(n+1)}{2}$

(D) $\frac{n(n-1)}{2}$

Roll No. _____ to be filled in by the candidate.

(For all sessions)

Mathematics (Essay Type)

Time: 2:30 Hours

Marks: 80

Section -I

2. Write short answers of any eight parts from the following.

2x8=16

- i. Separate into real and imaginary parts $\frac{i}{1+i}$.
- ii. Simplify $\left(\frac{-1}{2} - \frac{\sqrt{3}}{2}i\right)^3$.
- iii. Write the converse and inverse of $q \rightarrow p$.
- iv. Define the terms proper and improper subsets with example.
- v. Find inverse of $\begin{bmatrix} -2 & 3 \\ -4 & 5 \end{bmatrix}$.
- vi. Differentiate between I_n to and on to function.
- vii. For a square matrix A, $|A| = |A'|$.
- viii. What is Rank of matrix? Explain with example.
- ix. Solve $15x^2 + 2ax - a^2 = 0$ by quadratic formula.
- x. If α, β are roots of $3x^2 - 2x + 4 = 0$, find $\frac{\alpha}{\beta} + \frac{\beta}{\alpha}$.
- xi. Does the set $\{0, -1\}$ possess closure property w.r.t "Addition" and "multiplication"?
- xii. Show that roots of equation $(p+q)x^2 - px - q = 0$ are rational.

3. Write short answers of any eight parts from the following.

2x8=16

- i. Resolve into partial fractions $\frac{x^2+1}{x^2-1}$.
- ii. If $y = 1 + \frac{x}{2} + \frac{x^2}{4} + \dots \infty$, show that $x = \frac{2(y-1)}{y}$.
- iii. Prove that $\sum_{k=1}^n K = \frac{n(n+1)}{2}$.
- iv. Find n , if ${}^n P_2 = 30$.
- v. Find n , if ${}^n C_{10} = \frac{12 \times 11}{2!}$.
- vi. Define the probability.
- vii. If 5 and 8 are arithmetic means between a and b find a and b.
- viii. Find 12th term of Harmonic progression $\frac{1}{3}, \frac{2}{9}, \frac{1}{6}, \dots$
- ix. In how many ways 4 keys be arranged on a circular key ring?
- x. Prove the formula $1+3+5+\dots+(2n-1) = n^2$ for $n=1, 2$.
- xi. Find the term involving x^4 in the expansion of $(3-2x)^7$.
- xii. Use binomial theorem, find the value to three decimal places $(1.03)^{\frac{1}{3}}$.

4. Write short answers of any nine parts from the following.

2x9=18

- i. Verify $2 \sin 45^\circ + \frac{1}{2} \operatorname{cosec} 45^\circ = \frac{3}{\sqrt{2}}$.
- ii. Prove that: $\frac{2 \tan \theta}{1 + \tan^2 \theta} = 2 \sin \theta \cos \theta$.

iii. Prove that $\tan(45^\circ + A)\tan(45^\circ - A) = 1$.

iv. Prove that: $\frac{\sin 2\alpha}{1 + \cos 2\alpha} = \tan \alpha$.

v. Define period of a trigonometric function.

vi. Prove that $\gamma = (s - a)\tan \frac{\alpha}{2}$.

vii. Prove that $\tan^{-1} \frac{1}{4} + \tan^{-1} \frac{1}{5} = \tan^{-1} \frac{9}{19}$.

viii. Solve $\sin x + \cos x = 0$.

ix. Solve the trigonometric equation $\sec^2 \theta = \frac{4}{3}$.

x. Find the radius of the circle in which the arc of the central angle of measure 1 radian cut off an arc of length 35cm.

xi. If α, β be the angle of a triangle ABC then prove that $\cos\left(\frac{\alpha + \beta}{2}\right) = \sin \frac{\gamma}{2}$.

xii. Find the smallest angle of $\triangle ABC$, when $a = 37.34$, $b = 3.24$, $c = 35.06$.

xiii. Find area of triangle ABC given three sides $a = 18$, $b = 24$, $c = 30$.

Section -II

Note: Attempt any three questions from the following.

10x3=30

5. (a) Convert into logical form and prove by truth table of $(A \cap B)' = A' \cup B'$.

(b) Find the value of λ if given system has non-trivial solution

$$x_1 + 4x_2 + \lambda x_3 = 0, 2x_1 + x_2 - 3x_3 = 0, 3x_1 + \lambda x_2 - 4x_3 = 0$$

6. (a) If α, β are the roots of $x^2 - px - p - c = 0$, then prove that: $(1 + \alpha)(1 + \beta) = 1 - C$.

(b) Resolve into partial fraction $\frac{x^2 + a^2}{(x^2 + b^2)(x^2 + c^2)(x^2 + d^2)}$

7. (a) The sum of 9 terms of a A.P is 171 and its eighth term is 31. Find the series.

(b) If x is very nearly equal 1 then prove that: $px^p - qx^q = (p - q)x^{p+q}$.

8. (a) Find the value of remaining trigonometric function of $\sin \theta = -\frac{1}{\sqrt{2}}$

and the terminal arm of the angle is not in quad III.

(b) Prove that: $\frac{\sin 3\theta}{\cos \theta} + \frac{\cos 3\theta}{\sin \theta} = 2 \cot 2\theta$.

9. (a) Prove that: $r_1 + r_2 + r_3 - r = 4R$.

(b) Prove that: $\sin^{-1} \frac{3}{5} + \sin^{-1} \frac{8}{17} = \sin^{-1} \frac{77}{85}$.



Roll No. _____ to be filled in by the candidate.

(For all sessions)

Paper Code

6

1

9

1

Mathematics (Objective Type)

Time: 30 Minutes

Marks: 20

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given. Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. If $z = \cos \theta + i \sin \theta$, then $|z|$ is equal to:

(A) 0

(B) 1

(C) 2

(D) 3

2. For any two subsets A and B of set \cup , then $(A \cup B)'$ is equal to:(A) $A \cup B'$ (B) $A \cap B'$ (C) $A' \cup B'$ (D) $A' \cap B'$ 3. If "A" is a square matrix and $(\bar{A})' = -A$, then "A" is called:

(A) Skew Symmetric

(B) Symmetric

(C) Skew Hermitian

(D) Hermitian

4. If $A = \begin{bmatrix} 4 & x & 3 \\ 7 & 3 & 6 \\ 2 & 3 & 1 \end{bmatrix}$ is a singular matrix, then 'x' is equal to:

(A) 3

(B) 4

(C) 6

(D) 7

5. If α and β are roots of $ax^2 + bx + c = 0$, then $\alpha \cdot \beta$ is equal to:(A) $-b/a$ (B) a/b (C) c/a (D) a/c 6. If "w" is a cube root of unity, then $(1 + w - w^2)(1 - w + w^2)$ will be equal to:

(A) 3

(B) 4

(C) 2

(D) 1

7. If $\frac{3}{(x-1)(x+2)} = \frac{1}{x-1} + \frac{A}{x+2}$, then "A" is equal to:

(A) -1

(B) 3

(C) 2

(D) 4

8. The n^{th} root of product of n Geometric Means between a and b is equal to:(A) $(ab)^{1/n}$ (B) $a^n b^n$ (C) $n\sqrt{ab}$ (D) \sqrt{ab} 9. If in an A.P; $a_{n-3} = 2n - 5$, then a_n will be equal to:(A) $2n+1$ (B) $2n-1$ (C) $n+1$ (D) $n-1$ 10. $\frac{n!}{(n-r)!r!}$ is equal to:(A) ${}^r C_n$ (B) ${}^r P_n$ (C) ${}^n C_r$ (D) ${}^n P_r$

11. Number of signals given by 5 flags of different colours using 3 flags at a time equals.

- (A) 30 (B) 40 (C) 50 (D) 60

12. Sum of even co-efficient in the expansion of $(1+x)^n$ equals.

- (A) 2^{n+1} (B) 2^{n-1} (C) 2^n (D) 2^{1-n}

13. Third term in the expansion of $(1-2x)^{1/3}$ is equal to:

- (A) $-9x^2/4$ (B) $9x^2/4$ (C) $4x^2/9$ (D) $-4x^2/9$

14. The area of a sector of circular region of radius r and angle θ is equal to:

- (A) $\frac{1}{2}r\theta^2$ (B) $\frac{1}{2}r^2\theta$ (C) $r\theta^2$ (D) $r^2\theta$

15. If $6\cos^2\theta + 2\sin^2\theta = 5$, then $\tan^2\theta$ will be equal to:

- (A) $\frac{3}{2}$ (B) 3 (C) $\frac{1}{3}$ (D) $\frac{2}{3}$

16. Period of $\sin\frac{x}{5}$ is equal to:

- (A) 10π (B) 5π (C) 2π (D) $\frac{2\pi}{5}$

17. In an oblique triangle, if $a = 200$, $b = 120$ and included angle $\gamma = 150^\circ$, then its area will be equal to:

- (A) 6000 (B) 5000 (C) 2000 (D) 12000

18. If " R " is the circum-radius, then its value is:

- (A) $\frac{ac}{4\Delta}$ (B) $\frac{ab}{4\Delta}$ (C) $\frac{abc}{4\Delta}$ (D) $\frac{abc}{\Delta}$

19. The value of $\sin\left(\cos^{-1}\frac{\sqrt{3}}{2}\right)$ is equal to:

- (A) 1 (B) -1 (C) $\frac{-1}{2}$ (D) $\frac{1}{2}$

20. The solution of $\cos ec\theta = 2$ in interval $[0, 2\pi]$ is equal to:

- (A) $\frac{\pi}{6}, \frac{7\pi}{6}$ (B) $\frac{\pi}{6}, \frac{5\pi}{6}$ (C) $\frac{\pi}{3}, \frac{5\pi}{6}$ (D) $\frac{\pi}{3}, \frac{\pi}{6}$

Roll No. _____ to be filled in by the candidate.

(For all sessions)

Mathematics (Essay Type)

Time: 2:30 Hours

Marks: 80

Section -I

2. Write short answers of any eight parts from the following.

2x8=16

- i. Find the modulus of complex number $3 + 4i$.
- ii. Simplify by justifying each step $\frac{1}{1} + \frac{1}{1} = \frac{4}{4} + \frac{5}{5}$ by writing properties.
- iii. Factorize the expression $9a^2 + 16b^2$.
- iv. Define absurdity and give one example.
- v. Solve the system of linear equations. $\begin{cases} 4x_1 + 3x_2 = 5 \\ 3x_1 - x_2 = 7 \end{cases}$
- vi. Find the value of x if $\begin{vmatrix} 1 & 2 & 1 \\ 2 & x & 2 \\ 3 & 6 & x \end{vmatrix} = 0$.
- vii. Define Row Rank of a matrix.
- viii. Solve the equation $x^{-2} - 10 = 3x^{-1}$.
- ix. If $A = \{1, 2, 3, 4\}$, $B = \{3, 4, 5, 6, 7, 8\}$, $C = \{5, 6, 7, 9, 10\}$ verify distributivity of union over intersection.
- x. Find the inverse of the relation $\{(1, 3), (2, 5), (3, 7), (4, 9), (5, 11)\}$.
- xi. Use remainder theorem to find the remainder when $x^3 - x^2 + 5x + 4$ is divided by $x - 2$.
- xii. Find the roots of the equation $16x^2 + 8x + 1 = 0$ by using quadratic formula.

3. Write short answers of any eight parts from the following.

2x8=16

- i. Resolve $\frac{1}{x^2 - 1}$ into partial fraction.
- ii. Find 5th term of Geometric progression G.P 2, 6, 12,
- iii. Define Circular permutation.
- iv. Expand $(4 - 3x)^{\frac{1}{2}}$ upto three terms.
- v. If $\frac{1}{a}, \frac{1}{b}, \frac{1}{c}$ are in Arithmetic progression (A.P) show that common difference is $\frac{a - c}{2ac}$.
- vi. If 5, 6 are two Arithmetic Means (A.M) between "a" and "b". Find "a" and "b".
- vii. If the numbers $\frac{1}{k}, \frac{1}{2k+1}, \frac{1}{4k-1}$ are in (H.P) Harmonic Progression, Find "K".
- viii. How many words can be formed from the letters of "PLAN" using all letters when no letter is to be repeated?
- ix. If ${}^n C_5 = {}^n C_4$, where C stands for combination then find value of n .
- x. Verify the inequality $n > 2^n - 1$ for integral values of $n = 4, 5$.
- xi. If x is so small that its square and higher power can be neglected, show that $\frac{1-x}{\sqrt{1-x}} = 1 - \frac{3}{2}x$.
- xii. Prove that Harmonic Mean (H.M) between two numbers "a" and "b" is $\frac{2ab}{a+b}$.

4. Write short answers of any nine parts from the following.

2x9=18

- i. Prove the fundamental identity $\cos^2 \theta + \sin^2 \theta = 1$.
- ii. Verify the result $\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$ for $\theta = 30^\circ$.

iii. Show that $\frac{\cos 11^\circ + \sin 11^\circ}{\cos 11^\circ - \sin 11^\circ} = \tan 56^\circ$.

iv. Prove that $\cos 330^\circ \sin 600^\circ + \cos 120^\circ \sin 150^\circ = -1$.

v. Find the period of $\operatorname{cosec}(10x)$.

vi. Show that $\gamma = 4R \sin \frac{\alpha}{2} \sin \frac{\beta}{2} \sin \frac{\gamma}{2}$ with usual notation.

vii. Find the value of $\cos\left(\sin^{-1} \frac{1}{2}\right)$.

viii. Show that $\frac{\cot^2 \theta - 1}{1 + \cot^2 \theta} = 2 \cos^2 \theta - 1$.

ix. Express the following difference as the product of trigonometric functions $\cos 7\theta - \cos \theta$.

x. In any triangle $\triangle ABC$, if $c = 16.1, \alpha = 42^\circ 45', \gamma = 74^\circ 32'$, then find " β " and " α ".

xi. Find the area of triangle ABC, given two sides and their included angle $a = 200, b = 120, \gamma = 150^\circ$.

xii. Find the solutions of the equation $\cot \theta = \frac{1}{\sqrt{3}}$ in the interval $[0, 2\pi]$.

xiii. Find the values of θ satisfying the equation $3 \tan^2 \theta + 2\sqrt{3} \tan \theta + 1 = 0$.

Section -II

Note: Attempt any three questions from the following.

10x3=30

5. (a) Verify De Morgan's Laws for the given sets: $U = \{1, 2, 3, \dots, 20\}, A = \{2, 4, 6, \dots, 20\}, B = \{1, 3, 5, \dots, 19\}$.

(b) Find the value of λ if A is singular matrix, $A = \begin{bmatrix} 4 & \lambda & 3 \\ 7 & 3 & 6 \\ 2 & 3 & 1 \end{bmatrix}$.

6. (a) If the roots of $px^2 + qx + q = 0$ are α and β , then prove that $\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} + \sqrt{\frac{q}{p}} = 0$.

(b) Resolve into partial fraction $\frac{x^4}{1-x^4}$.

7. (a) The sum of an infinite geometric series is 9 and sum of square of its terms is $\frac{81}{5}$. Find the series.

(b) If $y = \frac{2}{5} + \frac{1.3}{2!} \left(\frac{2}{5}\right)^2 + \frac{1.3.5}{3!} \left(\frac{2}{5}\right)^3 + \dots$, then prove that $y^2 + 2y - 4 = 0$.

8. (a) A railway train is running on a circular track of radius 500 meters at the rate of 30Km per hour.

Through what angle will it turn in 10 sec?

(b) If $\tan \alpha = \frac{-15}{8}$ and $\sin \beta = \frac{-7}{25}$ and neither the terminal side of the angle of measure α nor that

of β is in IV quadrant. Find $\sin(\alpha + \beta)$ and $\cos(\alpha + \beta)$.

9. (a) One side of a triangular garden is 30m. If two corner angle are $22^\circ \frac{1}{2}$ and $112^\circ \frac{1}{2}$, find the cost of

planting the grass at the rate of Rs.5 per square meter.

(b) Prove that $\tan^{-1} \frac{3}{4} + \tan^{-1} \frac{3}{5} - \tan^{-1} \frac{8}{19} = \frac{\pi}{4}$.



Roll No. _____ to be filled in by the candidate.

(For all sessions)

Paper Code	6	1	9	1
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Mathematics (Objective Type)

Time: 30 Minutes

Marks: 20

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given. Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. Multiplicative identity of complex number is:

- (A) (0,0) (B) (0,1) (C) (1,0) (D) (1,1)

2. The contrapositive of $\sim p \rightarrow \sim q$ is:

- (A) $p \rightarrow q$ (B) $q \rightarrow p$ (C) $\sim q \rightarrow \sim p$ (D) $\sim q \rightarrow p$

3. If A and B are any two non singular matrices then $(AB)^{-1} =$

- (A) $A^{-1}B^{-1}$ (B) $B^{-1}A^{-1}$ (C) BA (D) AB

4. For a non-singular matrix A if $XA=B$ then $X =$

- (A) $A^{-1}B$ (B) BA^{-1} (C) $(AB)^{-1}$ (D) $(BA)^{-1}$

5. If $f(x) = 3x^4 + 4x^3 + x - 5$ is divided by $x+1$, then remainder is:

- (A) -6 (B) 7 (C) 6 (D) -7

6. If w is cube root of unity, then $w^{15} =$

- (A) 1 (B) 0 (C) w (D) -w

7. Partial fraction of $\frac{3x-11}{(x^2+1)(x+3)}$ will be of the form.

- (A) $\frac{Ax+B}{x^2+1} + \frac{C}{x+3}$ (B) $\frac{A}{x^2+1} + \frac{Bx+C}{x+3}$ (C) $\frac{Ax+B}{x+3} + \frac{C}{x^2+1}$ (D) $\frac{A}{x^2+1} + \frac{B}{x+3}$

8. If $a_n = (-1)^{n+1}$, then 26th term is:

- (A) 1 (B) -1 (C) 26 (D) -26

9. $(n+1)^{th}$ term of G.P is:

- (A) $a_1 r^{n-1}$ (B) $a_1 r^{n+1}$ (C) $a_1 r^{n+2}$ (D) $a_1 r^n$

10. n^{th} term of A.P is:

- (A) $a_1(n-1)d$ (B) $a_1 + (n+1)d$ (C) $2a_1 + (n-1)d$ (D) $a_1 + (2n-1)d$

11. With usual notation ${}^nC_r + {}^nC_{r-1} =$
- (A) ${}^nC_{r+1}$ (B) nC_r (C) ${}^nC_{r-1}$ (D) ${}^nC_{r-1}$
12. In the expansion of $(a+b)^7$, the second term is:
- (A) a^7 (B) $7a^6b$ (C) $7ab^6$ (D) 8
13. In one hour, the hour hand of a clock turns through an angle.
- (A) $\frac{\pi}{8}$ (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{6}$ (D) $\frac{\pi}{2}$
14. $3\frac{\pi}{4}$ radian is equal to:
- (A) 110° (B) 135° (C) 150° (D) 130°
15. $\sin(-300^\circ) =$
- (A) $-\frac{\sqrt{3}}{2}$ (B) $\frac{\sqrt{3}}{2}$ (C) $\frac{1}{2}$ (D) 0
16. Period of $\sin x$ is:
- (A) π (B) 2π (C) 3π (D) $-\pi$
17. Radius of escribed circle opposite to vertex C is:
- (A) $\frac{\Delta}{s-a}$ (B) $\frac{\Delta}{s-b}$ (C) $\frac{\Delta}{s-c}$ (D) $\frac{\Delta}{s}$
18. With usual notation $a+b-c =$
- (A) $2S$ (B) $2S-2C$ (C) $2S-2b$ (D) $2S-c$
19. $2 \tan^{-1} A =$
- (A) $\tan^{-1} \frac{2A}{1-A^2}$ (B) $\tan^{-1} \frac{2A}{1+A^2}$ (C) $\tan^{-1} \frac{A}{1-A^2}$ (D) $\tan^{-1} \frac{A}{1+A^2}$
20. Solution of $\cot \theta = \frac{1}{\sqrt{3}}$ in quadrant III is:
- (A) $\frac{5\pi}{3}$ (B) $7\frac{\pi}{6}$ (C) $\frac{4\pi}{3}$ (D) $\frac{7\pi}{3}$

Roll No. _____ to be filled in by the candidate.

(For all sessions)

Mathematics (Essay Type)

Time: 2:30 Hours

Marks: 80

Section -I

2. Write short answers of any eight parts from the following.

2x8=16

- i. Separate into real and imaginary parts $\frac{2-7i}{4+5i}$.
- ii. Factorize $3x^2 + 3y^2$.
- iii. Simplify $(2,6)(3,7)$.
- iv. Let $A = \{1,2,3,4\}$, Find the relation $\{(x,y) / x+y < 5\}$ in A .
- v. Write the inverse and converse of $\sim p \rightarrow \sim q$.
- vi. Find the value of x if $\begin{vmatrix} 3 & 1 & x \\ -1 & 3 & 4 \\ x & 1 & 0 \end{vmatrix} = -30$
- vii. Find the condition that one root of $x^2 + px + q = 0$ is multiplicative inverse of other.
- viii. Evaluate $(1+w+w^2)(1-w+w^2)$.
- ix. Solve the equation $ax = b$ where a, b are the elements of a group G .
- x. Discuss the nature of roots of the equation $2x^2 - 5x + 1 = 0$.
- xi. If $A = \begin{bmatrix} 1 & 2 \\ a & b \end{bmatrix}$ and $A^2 = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$ then find the values of a and b .
- xii. If A and B are square matrices of the same order, then explain why in general $(A+B)(A-B) \neq A^2 - B^2$.

3. Write short answers of any eight parts from the following.

2x8=16

- i. Which term of the A.P., $-2, 4, 10, \dots$ is 148?
- ii. Insert three G.M's between 1 and 16.
- iii. Write in factorial form $\frac{(n+1)(n)(n-1)}{3.2.1}$.
- iv. Find the value of n , when ${}^n P_4 : {}^{n-1} P_3 = 9:1$
- v. If 5 is the harmonic mean between 2 and b , find b .
- vi. Find the number of diagonals of a 6-sided figure.
- vii. Evaluate $\sqrt[3]{30}$ correct to two places of decimals.
- viii. Expand by binomial theorem $\left(\sqrt{\frac{a}{x}} - \sqrt{\frac{x}{a}}\right)^3$.
- ix. Resolve into partial fractions $\frac{7x+25}{(x+3)(x+4)}$.
- x. Resolve into partial fractions without finding the constants $\frac{9x-7}{(x^2+1)(x+3)}$
- xi. If $\frac{1}{a}, \frac{1}{b}$ and $\frac{1}{c}$ are in G.P, show that the common ratio is $\pm \sqrt{\frac{a}{c}}$.
- xii. Check whether, $1 + \frac{1}{2} + \frac{1}{4} + \dots + \frac{1}{2^{n-1}} = 2\left(1 - \frac{1}{2^n}\right)$ is true for $n = 1, 2$.

4. Write short answers of any nine parts from the following.

2x9=18

- i. Prove that $\sec^2 \theta - \operatorname{cosec}^2 \theta = \tan^2 \theta - \cot^2 \theta$. ii. Find the values of $\cos 105^\circ$ taking $(105^\circ = 45^\circ + 60^\circ)$.
- iii. Prove that $\frac{\sin 8x + \sin 2x}{\cos 8x + \cos 2x} = \tan(5x)$. iv. Find the period of $\tan(4x)$.
- v. Show that $\gamma = (s-c) \tan\left(\frac{\gamma}{2}\right)$. vi. In $\triangle ABC$ $a=3, b=6$ and $B=36^\circ 20'$ Find "b".
- vii. Find area of $\triangle ABC$ if $a=18, b=24$ and $c=30$. viii. Find the value of $\cos^{-1}\left(\frac{-1}{2}\right)$.
- ix. Solve the equation $1 + \cos x = 0$. x. Find the soln of equation $\sec x = -2$ which lies in $[0, 2\pi]$.
- xi. What is the circular measure of the angle between the hands of a watch at 4 'o' clock.
- xii. Find the values of remaining trigonometric functions when $\cos \theta = \frac{9}{41}$ and the terminal arm of the angle is in quad Iv
- xiii. If α, β and γ are angles of a triangle ABC then prove that $\tan(\alpha + \beta) + \tan \gamma = 0$.

Section -II

Note: Attempt any three questions from the following.

10x3=30

5. (a) If $A = \begin{bmatrix} 2 & -1 \\ 3 & 1 \end{bmatrix}$ verify that $(A^{-1})^t = (A^t)^{-1}$.

(b) Solve the system of equations $x + y = 5$; $\frac{2}{x} + \frac{3}{y} = 2$.

6. (a) Resolve $\frac{1}{(1-ax)(1-bx)(1-cx)}$ into partial fractions.

(b) For what value of n , $\frac{a^n + b^n}{a^{n-1} + b^{n-1}}$ is the positive Geometric Mean (G.M) between a and b.

7. (a) Prove that ${}^n C_r + {}^n C_{r-1} = {}^{n+1} C_r$.

(b) If x is so small that its cube and higher powers can be neglected then show that $\sqrt{\frac{1+x}{1-x}} \approx 1 + x + \frac{1}{2}x^2$.

8. (a) Two cities A and B lie on the equator such that their longitudes are 45°E and 25°W respectively. Find the distance between two cities, taking radius of earth as 6400 kms.

(b) Show that $\cos(\alpha + \beta)\cos(\alpha - \beta) = \cos^2 \alpha - \sin^2 \beta = \cos^2 \beta - \sin^2 \alpha$.

9. (a) The sides of a triangle are $x^2 + x + 1, 2x + 1$ and $x^2 - 1$. Prove that the greatest angle of the triangle is 120° .

(b) Prove that $2 \tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{1}{7}\right) = \frac{\pi}{4}$.